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## MADALGO seminar by Jeremy T. Finemann, Massachusetts Institute of Technology

## **Cache-Oblivious Streaming B-Trees**

The B-tree is the classic external-memory-dictionary data structure. The B-tree is typically analyzed in a two-level memory model (called the DAM or I/O model) in which internal memory of size *M* is organized into size-*B* blocks, and there is an arbitrarily large external memory.

The cost in the model is the number of block transfers between internal and external memory. An *N*-element B-tree supports searches, insertions, and deletions in  $O(\log_B N)$  block transfers.

In fact, there is a tradeoff between the cost of searching and inserting in external-memory dictionaries [Brodal, Fagerberg 03], and the B-tree achieves only one point on this tradeoff. A more general trade off is exhibited by their buffered B-tree.

This talk presents two points on the insert/search tradeoff for cache-oblivious (CO) data structures, the *cache-oblivious lookahead array (COLA)*, and the *shuttle tree*. The CO model is similar to the DAM model, except that the block size *B* and memory size *M* are unknown to the algorithm. The buffered B-tree is not cache oblivious---buffer sizes are chosen according to *B*.

The COLA implements searches in  $O(\log_2 N)$  I/Os and inserts in amortized  $O((\log_2 N) / B)$  I/Os. Notice that the searches are worse than in the B-tree by a  $\log_2 B$  factor, but the inserts are better by a  $B/\log_2 B$  factor. These bounds represent one optimal point on insert/search trade off space. In fact, when made into a cache-aware data structure, the *lookahead array* achieves the same trade off as the buffered B-tree.

The shuttle tree implements searches in the optimal  $O(\log_B N)$  block transfers. Inserts cost  $o(\log_B N)$  block transfers, improving on the B-tree by a superconstant factor.

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